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## A SIMPLE MODEL OF FLOW THROUGH A TREE CANOPY AND COMPARISON WITH LARGE-EDDY SIMULATIONS

- ▶ The presence of a canopy reduces the local wind speed, resulting in a slower rate of spread of a wildfire than in the open
- ▶ This phenomenon has a major impact on firefighting operations as accurate predictions of fire spread are required for managing the fire
- ▶ We want a reliable model of McArthur's wind reduction factor [1] from easily obtained input data

### HARMAN AND FINNIGAN'S CANOPY MODEL [2]

- ▶ Balance shear production of turbulence with the aerodynamic drag from the canopy, assuming all other factors (ie advection, viscous diffusion) are not important
- ▶ Analytical monotonic solutions possible assuming a dense (large drag) canopy with negligible variation in drag with height
- ▶ Assume that drag is related to the volume fraction occupied by vegetation
- ▶ Example plot of wind speed within and above a canopy is shown in figure 1(a)

### Variation of drag with height

- ▶ Non-uniform drag profiles can be important in some forests [3]
- ▶ We extend the Harman and Finnigan model to allow drag  $\alpha f(z)$  to vary with height and solve the equation numerically

$$\frac{d}{dz} \left( \frac{du}{dz} \right)^2 = \alpha f(z) u^2 \quad (1)$$

where  $\alpha = c_D/2l^2$ ,  $c_D$  is the drag coefficient and  $l$  is the mixing length

- ▶ Example plot is shown in figure 1(b)

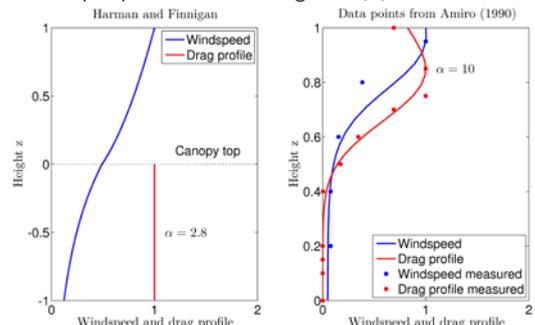


Figure 1 (a) left. Wind speed in and above a canopy according to the model of Harman and Finnigan. Figure 1 (b) right. Wind speed according to the extended model equation (1), compared with data from Amiro 1990 [4]. The parameter  $\alpha$  was estimated using the data in [4] and the method of Harman and Finnigan. The profiles have been normalised by maximum values.

### NUMERICAL SIMULATION OF A SIMPLE CANOPY

- ▶ We can conduct full numerical simulations over a modelled canopy (figure 2).
- ▶ Solve the full Navier-Stokes equations with the canopy represented by a drag force
- ▶ Use Large Eddy Simulation (LES) using Fire Dynamics Simulator [4]

$$F = c_D f(z) u^2$$

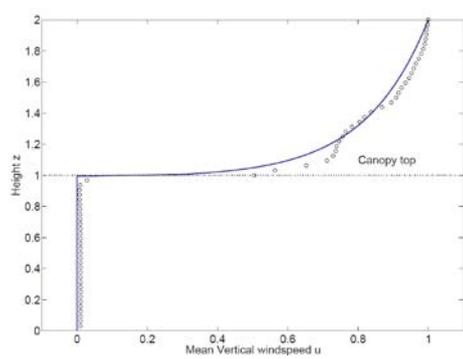


Figure 2 The mean vertical wind speed (circles) profile from a LES over a uniform canopy with  $c_D = 1$ . The blue line is the model of Harman and Finnigan. The velocity has been normalised to unity on the top of the domain. No slip boundary conditions are enforced at  $z = 0$ . Free slip boundary conditions are enforced at  $z = 2$ .

### LIMITATIONS OF THE SIMPLE MODEL

- ▶ Model appears to match observed data only if the canopy is sufficiently dense
- ▶ Need an estimate of  $\alpha$  and  $f(z)$ . Currently the estimates come from observations
- ▶ We can work towards models of  $f(z)$  for a canopy by constructing a model for a single tree

### LARGE EDDY SIMULATIONS OVER A SINGLE TREE

- ▶ It is possible model a canopy of trees by resolving the major branches of trees and using a subgrid scale model for the smallest branches and leaves
- ▶ ReNormalised Simulation (RNS) [5] has been developed to compute the drag of a fractal tree directly from simulated flows
- ▶ A fractal tree is a self similar object which resembles the complicated shape of a tree, but which have a simple standard description
- ▶ A pre-fractal tree is a fractal tree which has been truncated at some number of branch generations

- ▶ RNS has been applied to large canopies and validated against wind tunnel data
- ▶ Can be used to check the simple model and develop models of drag profile  $f(z)$

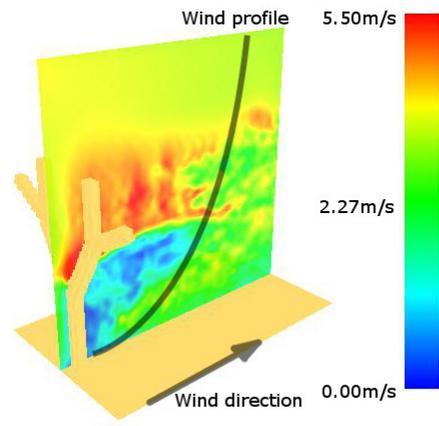


Figure 3. Simulation of the developing wake behind a two generation pre-fractal tree using an open source LES. code [4]. The domain is a box with a no slip boundary condition (BC) on the ground, an inflow BC on the left face, and outflow BCs on the other faces. A power law wind model is enforced in the direction shown. The instantaneous magnitude of velocity is shown at  $t=50s$ .

### FUTURE DIRECTIONS

- ▶ Verification of simple canopy model using numerical simulation over a fractal canopy (in progress)
- ▶ Development of a simple model of  $f(z)$  starting from models of single trees (in progress)
- ▶ Definition of a wind reduction factor by comparison to a canopy free wind
- ▶ Investigation of the effect of the canopy on the rate of spread of a fire

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 [5] Chester, S., Meneveau, C., & Parlange, M. B. (2007) *Journal of Computational Physics*, 225(1), 427-448.

